# ENERGY SAVING AND DISTANCE TRAVELED OF THE RAILWAY TRAIN FROM ITS BIRTH TO THE FOURTH INDUSTRIAL REVOLUTION MODELING 

DIMITRIOS A. ARVANITIDIS ${ }^{1 \text { 1a }}$, DIMITRIOS M. MASTRAKOULIS ${ }^{1}$ and IOANNIS DERVISIS ${ }^{2}$<br>${ }_{2}^{1}$ Science Department, University of Thessaly, Lamia 35100, Greece<br>${ }^{2}$ Department of Digital Systems, University of Piraeus 18534, Greece<br>Email: darvanitidis@uth.gr


#### Abstract

The simulation of railway systems plays a key role in the design of the supply of the railway network but also in the functionality of the train itself. Various studies have been carried out to understand the railway network and by extension the operation of the trains. [1,2] The history of the railway is an everlasting history of speed. The rail mode is a guided and low grip transit mechanism. Since the beginning of the Industrial Revolution at the start of the 19th century, when rail first emerged in Europe, passenger train speed has been crucial for competition-not necessarily with other kinds of transportation, but with other rail firms. Additionally, it gave verifiable proof of technological advancement in the time's most developed nations. In this work, an approach is studied for the modeling and simulation using Anylogic PLE regarding saving the energy and the distance traveled for five distinct time periods.


Key Words - train, railways, industrial period and simulation

## 1. Introduction

The purpose of this study is to simulate the movement of the train from its birth until today when we are going through the fourth industrial revolution and we are at the beginning of the fifth. In order to achieve this, typical examples of trains per industrial time period are used. Using the Anylogic PLE simulation software, the energy savings achieved per time period and also the distance traveled over time are examined. Finally, all the elements of the hypotheses in question are compared and contrasted in a common diagram.
The first workable steam locomotive was launched by Englishman Richard Trevithick in 1804, averaging less than 10 mph . $[1,3]$


Fig. 1 Richard Trevithick's steam locomotive | Museum Wales [3]

### 1.1 Before the Industrial Revolution

An Englishman named Sir Goldsworthy Gurney (17931875), who built steam-powered carriages more than 50 years before gasoline automobiles were invented. With breaks for water and fuel, the Gurney Steam Carriage Company traveled the London to Bath route in 1829 at an average pace of 14 miles per hour, which is nearly twice as fast as a horse-drawn coach.


Fig. 2 With top speeds of 20 mph , Gurney Steamers operated excursions to Edgeware, Barnet, and Stanmore. [4]

### 1.2 First Industrial Revolution

The two most important components in the railway - the track and the locomotive - were developed during the industrial revolution (1750-1840). George Stephenson built the first railway in the world in 1825 to connect the English cities of Stockton and Darlington. Coal was to be
transported along the railway. Steam engines were used to pull the carts. Horse-drawn carriages were used to transport passengers.


Fig. 3 George Stephenson and the Rocket locomotive [5]

### 1.3 Second Industrial Revolution

The combination of the steam engine and the rail at the beginning of the 19th century contributed tremendously to man's possibilities of high-speed travel. $6.5 \mathrm{~km} / \mathrm{h}$ for stagecoaches in 1840 compared to a commercial speed of roughly $60 \mathrm{~km} / \mathrm{h}$ for railroads as early as 1854 .


Fig. 4 Sierra Railway \#3 was built in 1891 and has a top speed of about 50 MPH [6]

### 1.4 Third or Digital Industrial Revolution

In 1973, the prototype HST British Rail Class 41 recorded a top speed of $143 \mathrm{mph}(230 \mathrm{~km} / \mathrm{h})$ in a test run the line. British legislation required the use of in-cab signaling for running at speeds more than $125 \mathrm{mph}(201 \mathrm{~km} / \mathrm{h})$ and so regular trains services were unable to run at such speeds. The lack of in-cab signaling was the primary reason that prevented the InterCity 225 trainsets from operating at their design speed of $140 \mathrm{mph}(225 \mathrm{~km} / \mathrm{h})$ during normal service. A secondary factor was that the signaling technology of the time was insufficient to allow detection of two broken rails on the running line. [7-9]


Fig. 5 British Rail Class 41 (HST) [10]

### 1.5 Fourth Industrial Revolution

The TGV (Train à Grande Vitesse) of France now holds the record for the fastest conventional wheeled passenger train, having attained $574.8 \mathrm{~km} / \mathrm{h}$ ( 357.2 mph ) over a 140 km ( 87 mi) section of track in 2007. [11]


Fig. 6 The French intercity high speed train called TGV (Train à Grande Vitesse). This specific engine set the world record for the fastest wheeled train on the 3 rd of April 2007. It reached an amazing speed of $574.8 \mathrm{~km} / \mathrm{h}$.
[12]

## 2. Description of Hypothesis and Simulation Process

Table 1. Description of Energies affecting positive the system [4]

| Value | Description of the Energies |
| :---: | :--- |
| Einv | This is the energy from the inverter. |
| Erec | This is the rectifier's energy. Substation losses can be produced <br> by the use of rectifiers and inverters with electricity (Esl). In <br> this study, it is assumed that the rectifier power efficiency <br> (_rec) and inverter power efficiency (inv), which have values <br> of 97\% and 95\%, respectively, are constants. |
| Ereg | The energy that can be used for regenerative braking is called <br> Ereg, while the energy that the brake rheostat expels is called <br> Eeb_r. The auxiliary system or the catenary system can <br> directly recycle and reuse some of the energy consumed by the <br> electro-braking system. However, excessive regeneration may <br> result in an increase in train voltage. The excess electro- <br> braking energy is absorbed by the braking rheostat in order to <br> shield the train from overvoltage. |
| Emr | This energy is the required amount to overcome motion <br> resistance. |
| Erec | This is the rectifier's energy. |
| Einv | This is the inverter's energy. |
| Ekin | This is the kinetic energy of the system. |

Table 2. Description of Energies affecting negative the system [4]

| Value | Description of the Energies |
| :--- | :---: |
| Erub | This is the Friction Energy. |


| Es | The railway receives its power from the AC electricity grid. After the traction substation energy has been corrected from the AC network, the excess regenerative braking energy can be reversed back into the AC network. This is the energy that was consumed. |
| :---: | :---: |
| EsI | To power moving trains, the DC catenary system receives electricity from substations. Transmission loss (Etl), which is caused by the current flowing through conductor rails, is dependent on both the resistance of the conductor rail (reconductor) and the amount of current flowing through it. This is the energy from the substation losses. |
| Etl | Moving trains are supplied with electricity by a DC catenary system that receives it from substations. Transmission loss (Etl), which is caused by the current flowing through conductor rails, is dependent on both the current and the resistance of the conductor rail (reconductor). This is the energy from the transmission losses. |
| $\begin{aligned} & \text { Etr_r } \\ & \text { Etr_e } \end{aligned}$ | The traction and auxiliary system use the train energy (Etr) from the DC catenary system. Onboard converters and motion resistance help to disperse some of the traction energy. The train gains kinetic energy, which is subsequently released by the braking mechanisms. This is the energy train $\pi 0 v \delta 1 \alpha \chi \omega \rho i \zeta \varepsilon \tau \alpha \iota$ $\sigma \varepsilon$ regenerative $\kappa \alpha \iota$ efficiency. |
| Ecl | This is the energy from the conversion losses. |
| Eeb | This is the energy from the electro-braking system. |
| Eaux | This is the energy from the auxiliary system. |
| Eeb_r | This is the energy that the brake rheostat has lost. |

## 3. Methodology

The grid of AC electricity supplies the railway with energy. After the traction substation energy has been corrected from the AC network, the excess regenerative braking energy can be reversed back into the AC network. Equation as below, where Erec is the energy from the rectifier and Einv is the energy from the inverter, can therefore be used to compute the overall system energy consumption (Es). [4]

$$
E_{s}=E_{r e c}-E_{i n v}
$$

Substation losses can be produced by the use of rectifiers and inverters with electricity (Esl). In this study, it is assumed that the rectifier power efficiency (rec) and inverter power efficiency (inv), which have values of $97 \%$ and $95 \%$, respectively, are constants. As a result, Equation can be used to compute the substation losses. [13,1]

$$
E_{s l}=E_{\text {rec }} \times\left(1-\eta_{r e c}\right)+E_{i n v} \times\left(1-\eta_{\text {inv }}\right)
$$

To power moving trains, the DC catenary system receives electricity from substations. Transmission loss (Etl), which is calculated by the resistance of the conductor rail (reconductor) and the current flowing through it using Equation, is produced by the current through conductor rails. [14,1]

$$
E_{t l}=\int r_{\text {conductor }} \times i^{2} d t
$$

The train energy (Etr) from the DC catenary system is used by the traction and auxiliary systems. Some of the traction energy is dispersed with the use of motion resistance and onboard converters. The train builds up kinetic energy, which the braking systems then release. The energy of the train can be stated in the form [15,1], where Ecl denotes conversion loss, Emr the energy needed to overcome motion resistance, Eeb the energy for the electro-braking system, and Eaux the energy for the auxiliary system.

$$
E_{t r}=E_{c l}+E_{m r}+E_{e b}+E_{a u x}
$$

The auxiliary system or the catenary system can directly recycle and reuse some of the energy consumed by the electro-braking system. However, an excessive amount of regeneration can raise the train voltage. The excess electrobraking energy is absorbed by the braking rheostat in order to shield the train from overvoltage. Equation [16,1], where Ereg is the usable regenerative braking energy and Eeb r is the energy lost by the braking rheostat, defines the regeneration efficiency (reg), which is used to assess the efficiency of regenerative braking energy.

$$
\eta_{r e g}=\frac{E_{r e g}}{E_{e b}}=\frac{E_{r e g}}{E_{e b \_r}+E_{r e g}}
$$

The total energy used by the entire system is equal to the sum of the energy lost during transmission, substation, and train operations, less regenerative braking energy. Thus, the energy flow from the level of the railway system should be in accordance with the energy conservation equation depicted in $[17,1]$. Complex interactions exist between the system energy flows. An extensive analysis of the infrastructural variables and operation controls is often required to estimate the energy flow characteristics of a feasible railway line.

$$
E_{r e c}-E_{i n v}=E_{s l}+E_{t l}+E_{t r}-E_{r e g}
$$

## 4. Methods and Energy consumption

Based on the assumptions and results of [1], for a case study that the speed restriction along stations is restricted to $40 \mathrm{~km} / \mathrm{h}$ and are included in the following table, a different scenario is examined.
The research in question will focus on the calculation of the power (energy) that a commercial train has per season. The division of the eras will be made according to the periods of the industrial revolution. Consequently, and taking into account the aforementioned the present research was carried out in order to investigate the difference and the evolution of

## Journal of Research in Engineering and Applied Sciences

the train of these time periods. As data regarding the speed of each train, the data obtained from research on the web and in particular the maximum value thereof (as recorded) were used. Below are the speeds after conversion to $\mathrm{km} / \mathrm{h}$.

Table 3. Maximum speed records per time period

| Time period | $\mathbf{M p h}$ | $\mathbf{K m} / \mathbf{h}$ |
| :---: | :---: | :---: |
| Before industrial revolution | 16 | 22.5308 |
| $1^{\text {st }}$ industrial revolution | 20 | 32.1869 |
| $2^{\text {nd }}$ industrial revolution | 37.2823 | 60 |
| $3^{\text {rd }}$ industrial revolution | 140 | 225.308 |
| $4^{\text {th }}$ industrial revolution | 357 | 574.8 |

Table 4. Energy consumption of the $40 \mathrm{~km} / \mathrm{h}$ case study.

| Scenario Index | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Auxiliary Power (kW) | 0 | 0 | 0 | 0 | 0 | 480 | 480 | 480 | 480 | 480 |
| Headway (s) | 90 | 100 | 120 | 300 | 600 | 90 | 100 | 120 | 300 | 600 |
| E, (kWh) | 802 | 796 | 825 | 840 | 845 | 2221 | 2221 | 2214 | 2199 | 2191 |
| $\mathrm{E}_{\text {rec }}(\mathrm{kWh})$ | 816 | 803 | 859 | 957 | 1066 | 2221 | 2221 | 2215 | 2209 | 2224 |
| $\mathrm{E}_{\text {inv }}(\mathrm{kWh})$ | -14 | -8 | -34 | -117 | -222 | 0 | 0 | 0 | -10 | -34 |
| $\mathrm{E}_{51}(\mathrm{kWh})$ | 25 | 24 | 28 | 35 | 44 | 67 | 67 | 66 | 67 | 69 |
| $\mathrm{E}_{\mathrm{f}}(\mathrm{kWh})$ | 16 | 13 | 17 | 12 | 10 | 84 | 73 | 67 | 33 | 21 |
| $\mathrm{E}_{\mathrm{tl}}(\mathrm{kWh})$ | 48 | 46 | 65 | 74 | 74 | 74 | 72 | 81 | 72 | 74 |
| $\mathrm{E}_{\text {tr_demand }}(\mathrm{kWh})$ | 1507 | 1507 | 1507 | 1507 | 1507 | 1507 | 1507 | 1507 | 1507 | 1507 |
| $\mathrm{E}_{\mathrm{t}_{( }(\mathrm{kWh})}$ | 1507 | 1507 | 1506 | 1507 | 1507 | 1476 | 1489 | 1479 | 1507 | 1507 |
| $\mathrm{E}_{\text {eb }}(\mathrm{kWh})$ | 796 | 796 | 796 | 796 | 796 | 796 | 796 | 796 | 796 | 796 |
| $\mathrm{E}_{\text {reg }}(\mathrm{kWh})$ | 794 | 795 | 791 | 788 | 790 | 796 | 796 | 796 | 796 | 796 |
| $\mathrm{Esaxx}^{\text {(kWh}}$ ) | 0 | 0 | 0 | 0 | 0 | 1316 | 1316 | 1316 | 1316 | 1316 |
| $\eta_{\text {reg }}$ | 100\% | 100\% | 99\% | 99\% | 99\% | 100\% | 100\% | 100\% | 100\% | 100\% |
| Time of under-voltage (s) | 0 | 0 | 8 | 0 | 0 | 312 | 192 | 250 | 3 | 0 |
| Time of train running (s) | 9900 | 9900 | 9900 | 9900 | 9900 | 9900 | 9900 | 9900 | 9900 | 9900 |

Table 5. Energy consumption of the $40 \mathrm{~km} / \mathrm{h}$ case study.

| Parameters | Value/Equation |
| :---: | :---: |
| Train mass with passengers, tonnes | 301 |
| Train formation | 3 M 3 T |
| Train length, m | 148 |
| Rotary allowance | 0.08 |
| Train Resistance, $\mathrm{N} /$ tonne | $3.49+0.039 \mathrm{v}+0.00066 \mathrm{v}^{2}(\mathrm{v}: \mathrm{km} / \mathrm{h})$ |
| Maximum traction and braking power, kW | 2518 |
| Maximum operation speed, $\mathrm{km} / \mathrm{h}$ | 80 |
| Maximum traction effort, kN | 351 |

The parameters used for the calculations are as follows [18]:

Table 6. Energy consumption of the $40 \mathrm{~km} / \mathrm{h}$ case study.

| Name | Type - Value | Explanation |
| :---: | :---: | :---: |
| g | 9.81 | Acceleration of gravity in $\mathrm{m} / \mathrm{s}^{2}$ |
| m | 301000 | Measurement in kg |
| $\mu \_\mathrm{k}$ | 0.57 | Sliding friction constant |
| $\mu_{-} \mathrm{s}$ | 0.75 | Constant of static friction |
| v 0 | 22.5308 | Train speed in IIoT |
| v 1 | 32.1869 | Train speed in IioT1 |
| v 2 | 60 | Train speed in IioT2 |
| v 3 | 225.308 | Train speed in IioT3 |
| v 4 | 574.8 | Train speed in IioT4 |

The values of the forces acting on the system and by extension the total energy produced are shown in the following table. The values already assigned to some of the actions below derive from the average of the ten scenarios in Table 4:

Table 7. Explanation of Energies affecting the system

| Name | Type - Value | Explanation |
| :---: | :---: | :---: |
| Erub | $\mu_{-} \mathrm{k}^{*} \mathrm{~m}^{*} \mathrm{~g}$ | Energy produced by the force of sliding <br> friction |
| Etr_e | 1507 | Energy produced by the train (divided |


| Etr_r | 1499.2 | into regenerative and efficiency) |
| :---: | :---: | :---: |
| Esl | 49.2 | Energy produced by the electricity <br> generated from substations |
| Erec | 1559.1 | Energy produced from the electricity <br> generated through rectifiers and inverters <br> that can generate substation losses |
| Es | 1515.4 | Energy produced from the traction <br> substation |
| Etl | 68 | Energy produced because of the current <br> that goes through conductor rails and <br> generates transmission loss, which is <br> determined by the resistance of the <br> conductor rail |
| Ereg | 793.8 | Energy produced by the useable <br> regenerative braking |
| Einv | -411 | Energy produced from the inverter |

Since the actions developed until the end of the movement are differentiated by means of movement and are divided into three distinct movements (beginning of movement, intermediate movement, end of movement). More specifically:

Table 8. Description of the forces and flows at the beginning of the process

| Name | Type - Value | Explanation |
| :---: | :---: | :---: |
| Ein | Ereg | Equals to the initial energy of the system <br> (same for all trains examined) |
| IIoT | $\mathrm{E}_{\text {IIoT }}$ | Equals to initial energy given $\mathrm{E}_{\text {in }}$ |
| IIoT1 | $\mathrm{E}_{\text {IIoT1 }}$ | Equals to initial energy given $\mathrm{E}_{\text {in }}$ |
| IIoT2 | $\mathrm{E}_{\text {IIoT2 }}$ | Equals to initial energy given $\mathrm{E}_{\text {in }}$ |
| IIoT3 | $\mathrm{E}_{\text {IIoT3 }}$ | Equals to initial energy given $\mathrm{E}_{\text {in }}$ |
| IIoT4 | $\mathrm{E}_{\text {IIIT4 }}$ | Equals to initial energy given $\mathrm{E}_{\text {in }}$ |
| $\mathrm{E}_{\text {kin }}$ | $\mathrm{m}^{*} \mathrm{~V}_{0} * \mathrm{~V}_{0}{ }^{*} 1 / 2$ | The kinetic energy of the train at state 0 |
| $\mathrm{E}_{\text {kin1 }}$ | $\mathrm{m}^{*} \mathrm{~V}_{1} * \mathrm{~V}_{1} * 1 / 2$ | The kinetic energy of the train at state 1 |
| $\mathrm{E}_{\text {kin2 }}$ | $\mathrm{m}^{*} \mathrm{~V}_{2} * \mathrm{~V}_{2} * 1 / 2$ | The kinetic energy of the train at state 2 |
| $\mathrm{E}_{\text {kin3 }}$ | $\mathrm{m}^{*} \mathrm{~V}_{3} * \mathrm{~V}_{3} * 1 / 2$ | The kinetic energy of the train at state 3 |
| $\mathrm{E}_{\text {kin4 }}$ | $\mathrm{m}^{*} \mathrm{~V}_{4} * \mathrm{~V}_{4}{ }^{*} 1 / 2$ | The kinetic energy of the train at state 4 |

Table 9. Description of the forces and flows until the end of the process

| Name | Type - Value | Explanation |
| :---: | :---: | :---: |
| IIoTE | IIoT | The flow to E0 |
| IIoTE1 | IIoT1 | The flow to E1 |
| IIoTE2 | IIoT2 | The flow to E2 |
| IIoTE3 | IIoT3 | The flow to E3 |
| IIoTE4 | IIoT4 | The flow to E4 |
| En0 | En0E0 = Etr_r+Erub | Determines the amount of <br> energy opposing the move of <br> the train |
| En1 | En1E1 = Etr_r+Erub | Determines the amount of <br> energy opposing the move of <br> the train |
| En2 | En2E2 $=$ <br> Esl+Etr_e + Etl+Erub | Determines the amount of <br> energy opposing the move of <br> the train |
| En3 | En3E3 $=$ <br> Es1+Etr_e + Etl+Erub | Determines the amount of <br> energy opposing the move of <br> the train |
| Ep0 | En4E4 $=$ <br> Ep0E0 $=$ Ereg+Ekin | Determines the amount of <br> energy opposing the move of <br> the train |
| Detetl+Erub | Determines the amount of <br> energy assisting the train to <br> move |  |


| Ep1 | Ep1E1 $=$ Ereg+Ekin1 | Determines the amount of <br> energy assisting the train to <br> move |
| :---: | :---: | :---: |
| Ep2 | Ep2E2 $=$ <br> Es+Einv+Erec+Ereg+Ekin2 | Determines the amount of <br> energy assisting the train to <br> move |
| Ep3 | Ep3E3 $=$ <br> Es+Einv+Erec+Ereg+Ekin3 | Determines the amount of <br> energy assisting the train to <br> move |
| Ep4 | Ep4E4 $=$ <br> Es+Einv+Erec+Ereg+Ekin4 | Determines the amount of <br> energy assisting the train to <br> move |
| s0 | E0/15 | Distance traveled for the time <br> of 15h |
| s1 | E2/15 | Distance traveled for the time <br> of 15h |
| s2 | E3/15 | Distance traveled for the time <br> of 15h |
| s3 | E4/15 | Distance traveled for the time <br> of 15h |
| s4 | Epistance traveled for the time |  |
| of 15h |  |  |



Fig. 7 Simulation Model


Fig. 8 Diagram of the actions developed at $\mathrm{t}=7.5 \mathrm{~h}$ (mid-motion)


Fig. 9 Diagram of the distance traveled by train type at $\mathrm{t}=7.5 \mathrm{~h}$ (midway)


- Ein - en eet ee2 - e3 ex

Fig. 10 Diagram of the actions developed at $\mathrm{t}=15 \mathrm{~h}$ (after motion)


Fig. 11 Diagram of the distance traveled by medium at $\mathrm{t}=15 \mathrm{~h}$ (after movement)

## 5. Conclusion

In this paper, a holistic modeling and simulation method was presented to evaluate the train and its progress through the industrial revolutions that followed its creation. The whole process concerns the movement of the train including those affecting the power system on a case-by-case basis, taking into account the different characteristics that each era had (coal, electricity, etc.) as well as the exclusion of thermal losses that may be applied by their nature to the drone.

At the end of the simulation, the distance traveled by each train was calculated in proportion to the speed it manages to develop. The simulation has been run for a duration of 15 minutes of train movement. The study in question was based on the study of [19], which is essentially based on a subway line in Singapore. The results suggest that the train of the 1st industrial revolution is superiorly faster and consequently the energy it gathers at the end of the movement, than what first appeared in the middle of the 19th century and in particular E1 $\approx 2.13 * E 0$.

The trains of the 1st and 2nd Industrial revolutions show several similarities, even E2 $\approx 3.5747 *$ E1, that is, almost four times as much energy was produced during the movement of the train of the 2 nd Industrial revolution.
Regarding the rest of the results, it can be seen that $\mathrm{E} 3 \approx 14.25 * \mathrm{E} 2$ while $\mathrm{E} 4 \approx 6.512 * \mathrm{E} 3$. In conclusion, the 3rd industrial revolution was launched compared to the previous ones and this is obviously due to the appearance of electricity in the first place but also to the increase in speed

## Journal of Research in Engineering and Applied Sciences

which results in the almost nullification of the resistance forces acting on the system.

Finally, the difference between the train of the 4th industrial revolution compared to the one that first appeared in the year 1804 lies in E4 $\approx 706.8^{*} \mathrm{E} 0$, which is due to the aforementioned appearance of electricity but also to the improvement of construction materials.

The reliability of a modern train can be assessed and anticipated based on simulation and evaluation, which can be investigated in the future. It is possible to examine and optimize the health and useable life of support and maintenance equipment by improving train operation and infrastructure design.

## 6. References

[1] Zhongbei Tian, Traction Power Substation Load Analysis with Various Train Operating Styles and Substation Fault Modes. Energies 2020.
[2] Alessandro Severino, Routes Planning Models for Railway Transport Systems in Relation to Passengers' Demand, Sustainability 13(16):8686, August 2021
[3] https://museum.wales/articles/1012/Richard-Trevithickrsquos-steamlocomotive/
[4] https://gurneyjourney.blogspot.com/2011/01/goldsworthy-gurneys-steam-carriages.html
[5] https://en.wikipedia.org/wiki/Stephenson\'s Rocket
[6] https://www.historycentral.com/Industrialage/SepButEqual.html
[7] "Testing the prototype HST in 1973". traintesting.com. Archived from the original on 15 September 2009. Retrieved 29 April 2009.
[8] Barnett, Roger (June 1992). "British Rail's InterCity 125 and 225" (PDF). UCTC Working Paper No. 114. University of California Transportation Center; University of California, Berkeley: 32.

Archived from the original (PDF) on 29 May 2008. Retrieved 27 May 2008.
[9] Heath, Don (August 1994). "Electrification of British Rail's East Coast Main Line". Paper No. 105. Proceedings of the Institute of Civil Engineers (Transportation): 232.
[10] https://en.wikipedia.org/wiki/British_Rail_Class_41 (HST)
[11] "French train breaks speed record". CBC News. 3 April 2007. Retrieved 1 October 2013.
[12] https://en.wikipedia.org/wiki/Railway speed record
[13] Tian, Z.; Weston, P.; Zhao, N.; Hilmansen, S.; Roberts, C.; Chen, L. System energy optimisation strategies for metros with regeneration Transp. Res. Part C Emerg. Technol. 2017, 75, 120-135.
[14] Lin, S.; Huang, D.; Wang, A.; Huang, Y.; Zhao, L.; Luo, R.; Lu, G. Research on the Regeneration Braking Energy Feedback System of Urban Rail Transit. IEEE Trans. Veh. Technol. 2019, 68, 7329-7339.
[15] Zhang, G.; Tian, Z.; Tricoli, P.; Hillmansen, S.; Liu, Z. A new hybrid simulation integrating transient-state and steady-state models for the analysis of reversible DC traction power systems. Int. J. Electr. Power Energy Syst. 2019, 109, 9-19.
[16] Zhang, G.; Tian, Z.; Tricoli, P.; Hillmansen, S.;Wang, Y.; Liu, Z. Inverter Operating Characteristics Optimization for DC Traction Power Supply Systems. IEEE Trans. Veh. Technol. 2019, 68, 3400 3410.
[17] Zhang, G.; Tian, Z.; Du, H.; Liu, Z. A Novel Hybrid DC Traction Power Supply System Integrating PV and Reversible Converters. Energies 2018, 11, 1661.
[18] https://el.wikipedia.org/wiki/\�\�\�\�\�\�\�\� \%CE\%AE
[19] Chymera, M.Z.; Renfrew, A.C.; Barnes, M.; Holden, J. Modeling Electrified Transit Systems. IEEE Trans. Veh. Technol. 2010, 59, 2748-2756.

